

Zero-Knowledge After Prime Time -- Proving Statements Over \mathbb{Z}_k

Abstract

Zero-knowledge proof systems are usually specified for computation over finite fields \mathbb{F}_2 or \mathbb{F}_p for large primes p . On the other hand, all modern CPUs operate on 32 bit or 64 bit integers, which naturally map to rings \mathbb{Z}_k . Although \mathbb{Z}_k -arithmetic can be emulated using prime moduli, this comes with an unavoidable overhead. Hence, it is desirable to have proof systems natively support computation over \mathbb{Z}_k . Constructing and proving efficient and sound protocols for \mathbb{Z}_k is however challenging, as many of the cryptographers favorite tools do not work over rings. We have to deal with zero divisors and misbehaving polynomials. This talk focuses on zero-knowledge proofs based on Vector Oblivious Linear Evaluation (VOLE) and the MPC-in-the-Head (MitH) paradigm. We show how to construct efficient VOLE over \mathbb{Z}_k based on a variant of Learning Parity with Noise (LPN) and discuss different methods to verify multiplications over \mathbb{Z}_k in the VOLE-ZK and MitH settings.

The talk is based on the following papers:

- Appenzeller to Brie: Efficient Zero-Knowledge Proofs for Mixed-Mode Arithmetic and \mathbb{Z}_k with Carsten Baum, Alexander Munch-Hansen, Benoit Razet, and Peter Scholl (CCS'21, <https://ia.cr/2021/750>)
- Mozzarella: Efficient Vector-OLE and Zero-Knowledge Proofs Over \mathbb{Z}_k with Carsten Baum, Alexander Munch-Hansen, and Peter Scholl (Crypto'22, <https://ia.cr/2022/819>)
- ZK-for- \mathbb{Z}_k : MPC-in-the-Head Zero-Knowledge Proofs for \mathbb{Z}_k with Cyprien Delpech de Saint Guilhem, Robin Jadoul, Emmanuela Orsini, Nigel P. Smart, and Titouan Tanguy (IMACC'23, <https://ia.cr/2023/1057>)

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